



**ICT in SES**

# Squares and cubes

Lesson №10

# Square and rectangle

# Square in Suica

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## Square

- Graphical object with properties
- Used to draw a square

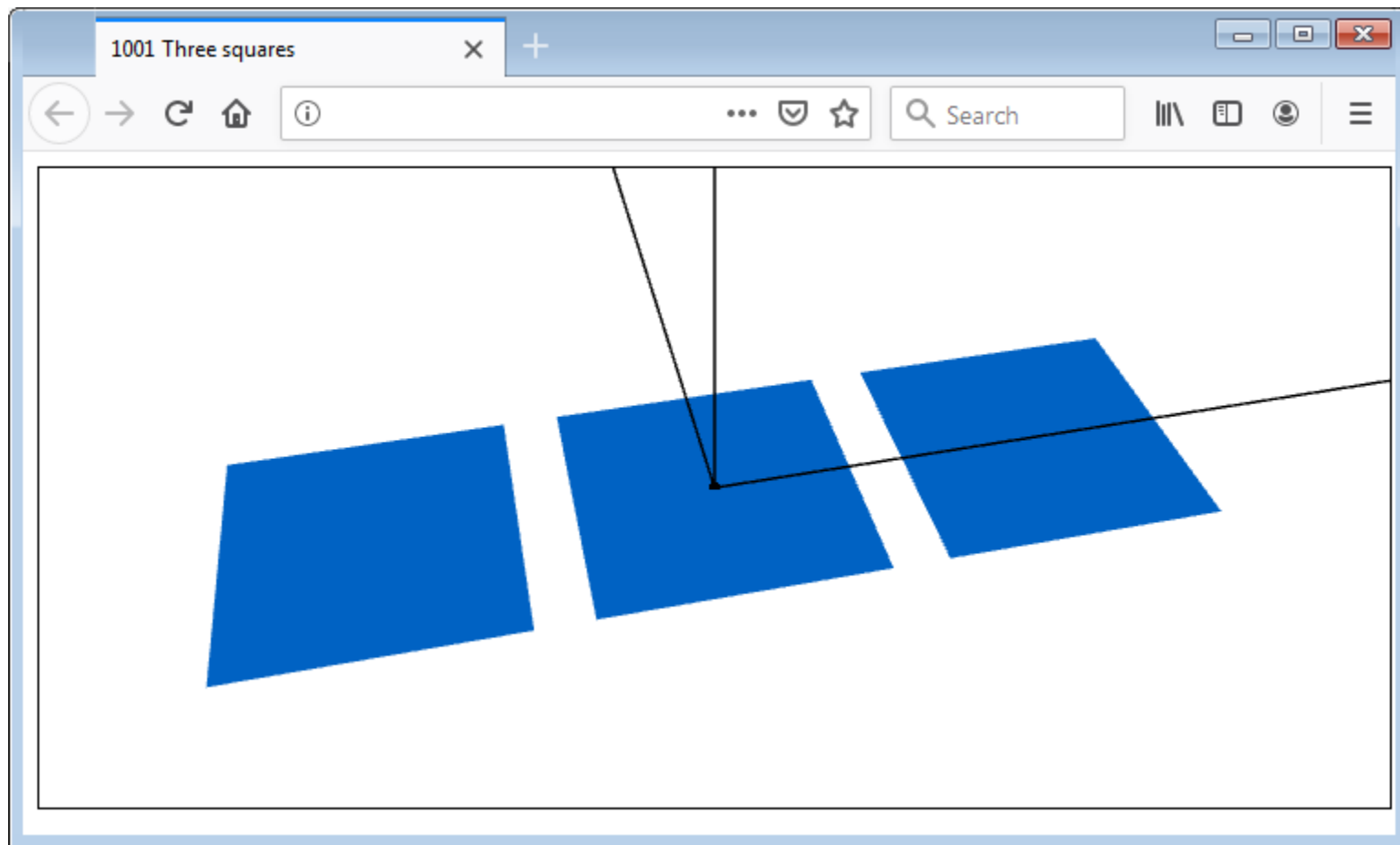
## Creating a square

- With class `new Suica.Square ( center, size )`
- With function `square ( center, size )`
- Center is coordinates of a point, an array of three numbers
- Size is a number, the length of the cube edge

# Example

- Create three squares in a row
- They have equal sizes
- There is some distance between them

```
square([-6,0,0],5);  
square([ 0,0,0],5);  
square([+6,0,0],5);
```



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# Properties

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## Drawing mode

- Optional property
- Stored in **mode**
- Defines how the square is draw
  - **Suica.POINT** drawn are the vertices
  - **Suica.LINE** drawn are the edges
  - **Suica.SOLID** drawn is a full square (default mode)

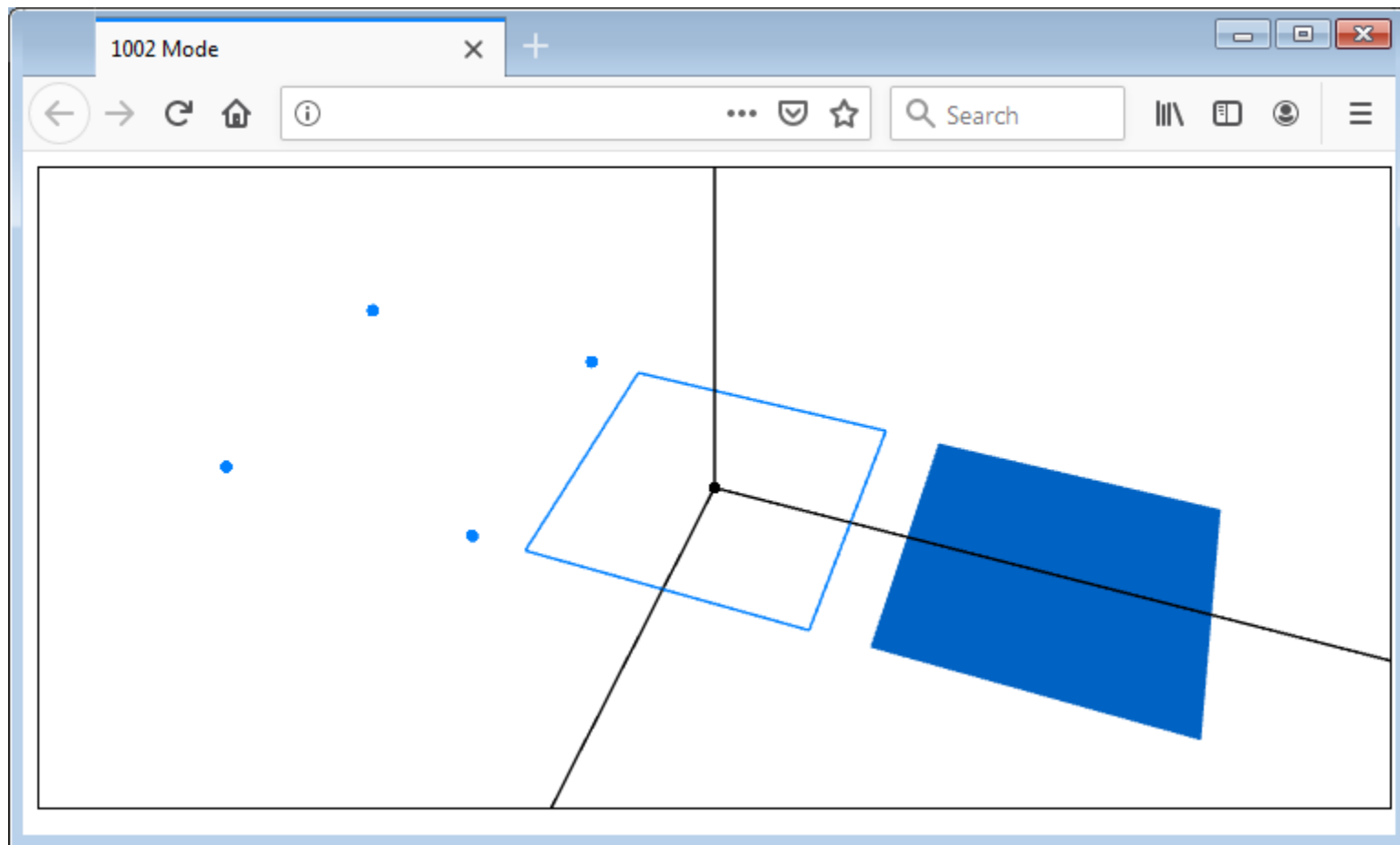
# Example

- Three squares using three drawing modes

```
a = square([0,-6,0],5);  
a.mode = Suica.POINT;  
a.pointSize = 7;
```

```
a = square([0,0,0],5);  
a.mode = Suica.LINE;
```

```
a = square([0,6,0],5);  
a.mode = Suica.SOLID;
```



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# Origin

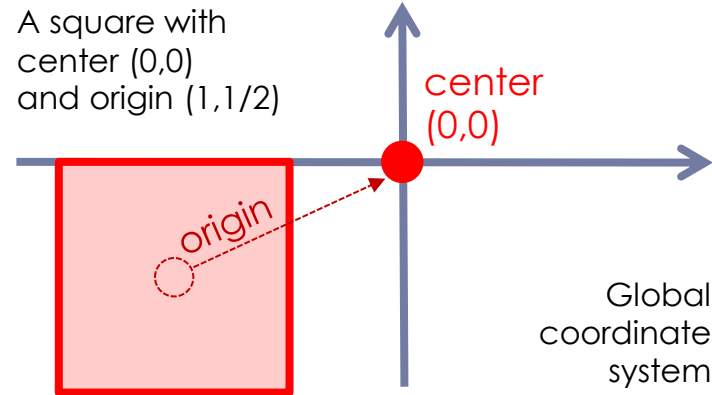
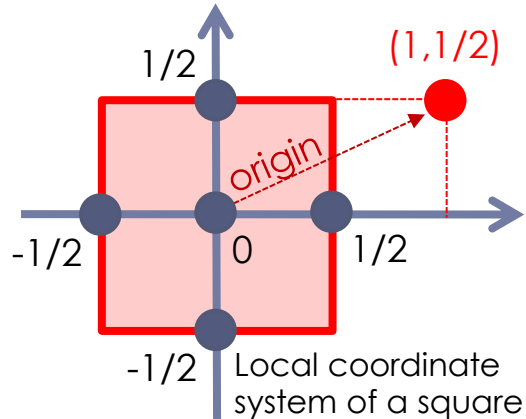
- Optional property
- Store in **origin**
- Defines the “center” of an object

## Purpose of origin

- In some cases it is easier to define location of a square via its vertex or edge middle point
- The property origin provides this functionality
- By default origin is (0,0,0) – thus the center of a square is the same as its geometrical middle point

# Coordinates in origin

- Measured in the local coordinate system of the object  
Origin = the geometrical center of the square  
Unit = the size of the square
- When a square is drawn, its origin is placed at the point, specified in the parameters for the square center



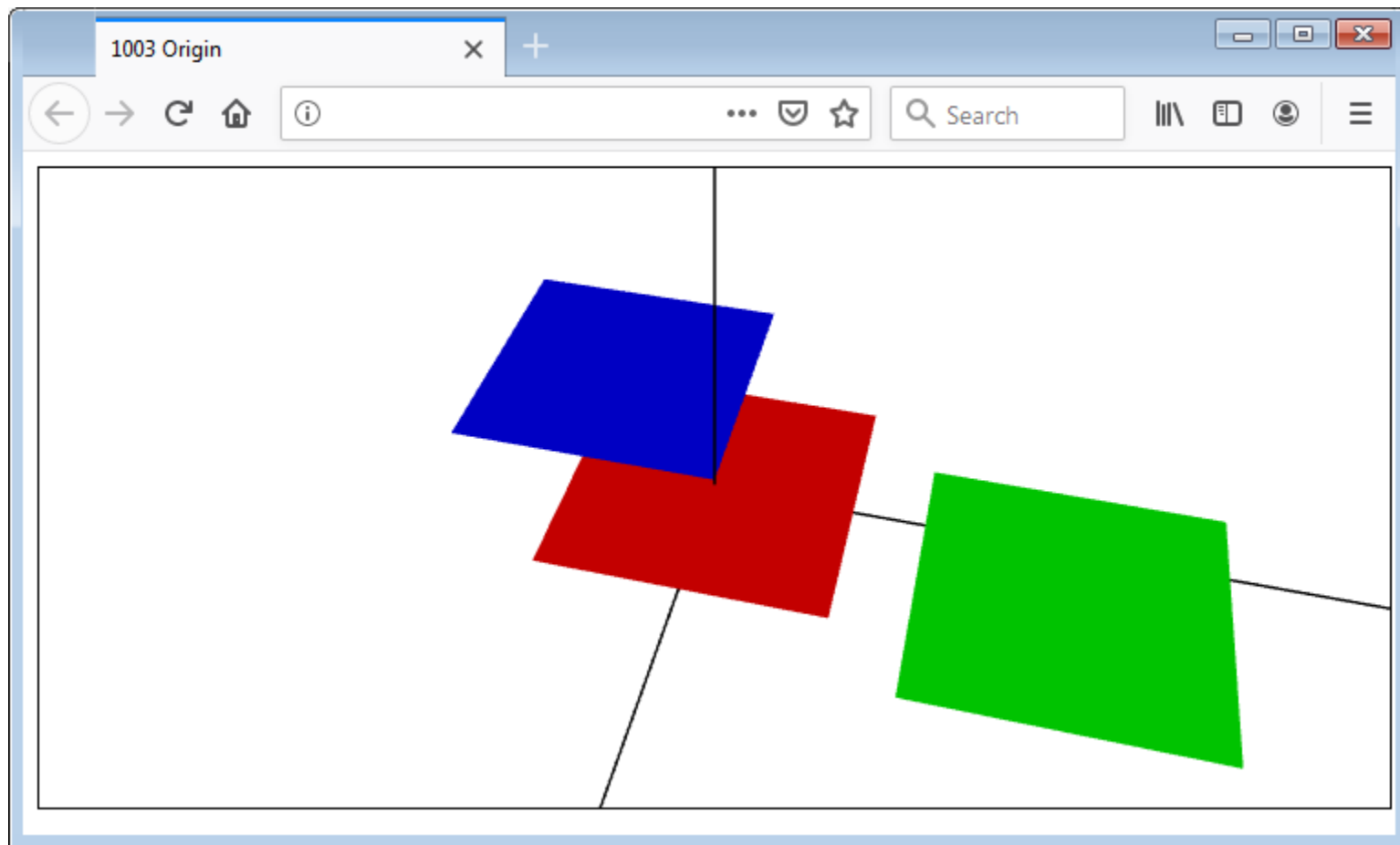
# Example

- Squares with origins  $(0,0,0)$ ,  $(1/2,1/2,0)$  и  $(-1/4,5/4,0)$

```
a = square([0,0,0.1],5);  
a.color = [1,0,0];
```

```
a = square([0,0,0.2],5);  
a.origin = [0.5,0.5,0];  
a.color = [0,0,1];
```

```
a = square([0,0,0.1],5);  
a.origin = [-0.25,-1.25,0];  
a.color = [0,1,0];
```



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# Rectangle in Suica

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## Rectangle

- Graphical object with properties similar to the square
- Used to draw squares and rectangles

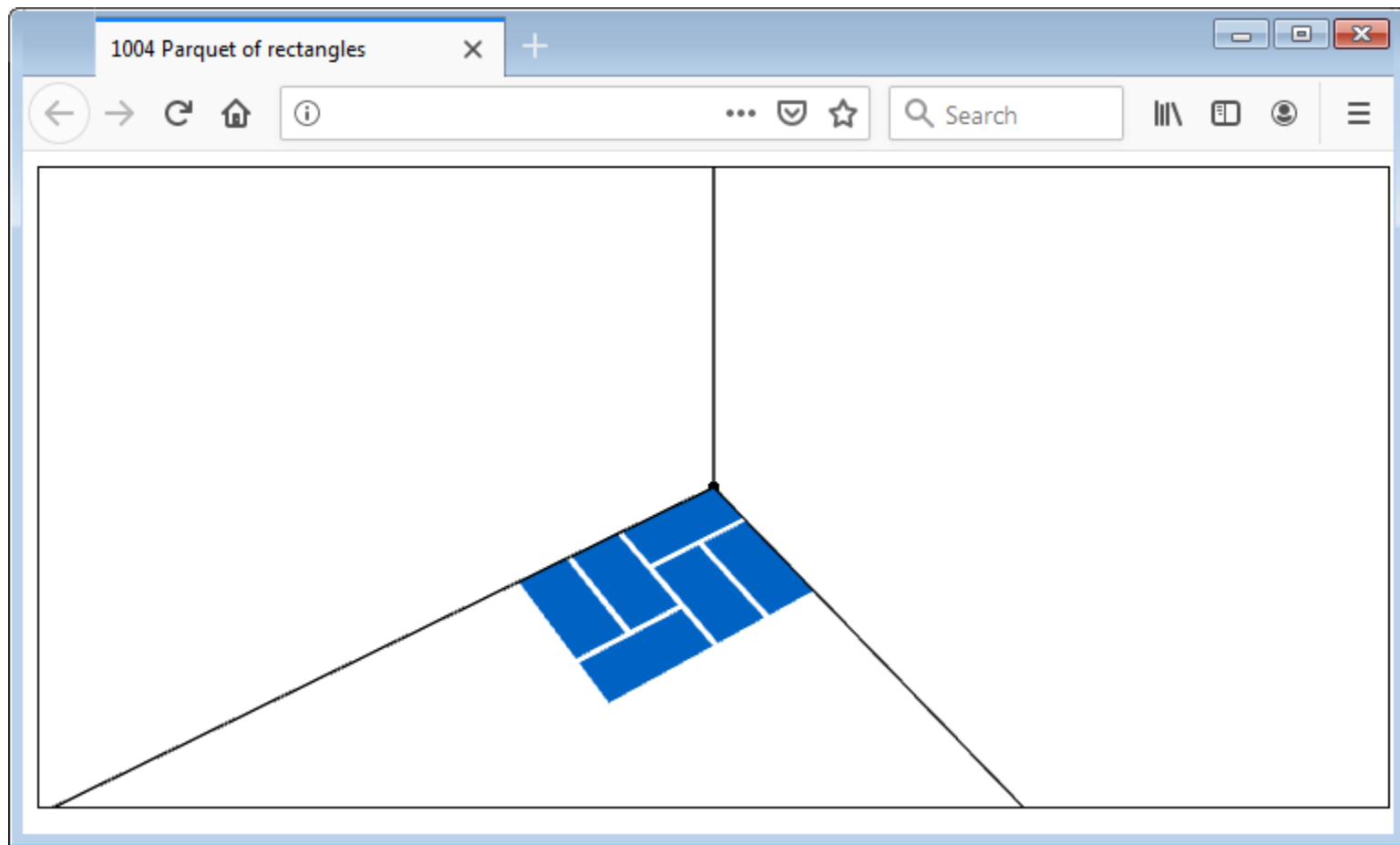
## Creating a rectangle

- With class `new Suica.Rectangle ( center, sizes )`
- With function `rectangle ( center, sizes )`
- Center is coordinates of a point, an array of three numbers
- Sizes is an array of 2 numbers – lengths of rectangle's sides

# Example

- A parquet of rectangles 2x1
- For easier positioning the centers are at the vertices
- The actual sizes are 1.9x0.9 to leave a tiny gap

```
a = rectangle([0,0,0],[1.9,0.9]);  
a.origin = [-0.5,-0.5,0];  
  
a = rectangle([0,1,0],[0.9,1.9]);  
a.origin = [-0.5,-0.5,0];  
  
a = rectangle([1,1,0],[0.9,1.9]);  
a.origin = [-0.5,-0.5,0];  
:
```



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# Cube and cuboid



# Cube in Suica

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## Cube

- Graphical objects with properties
- Used to draw a cube

## Creating a cube

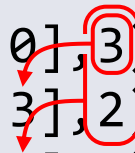
- With class `new Suica.Cube ( center, size )`
- With function `cube ( center, size )`
- Center is coordinates of a point, an array of three numbers
- Size is a number for the length of the cube edge

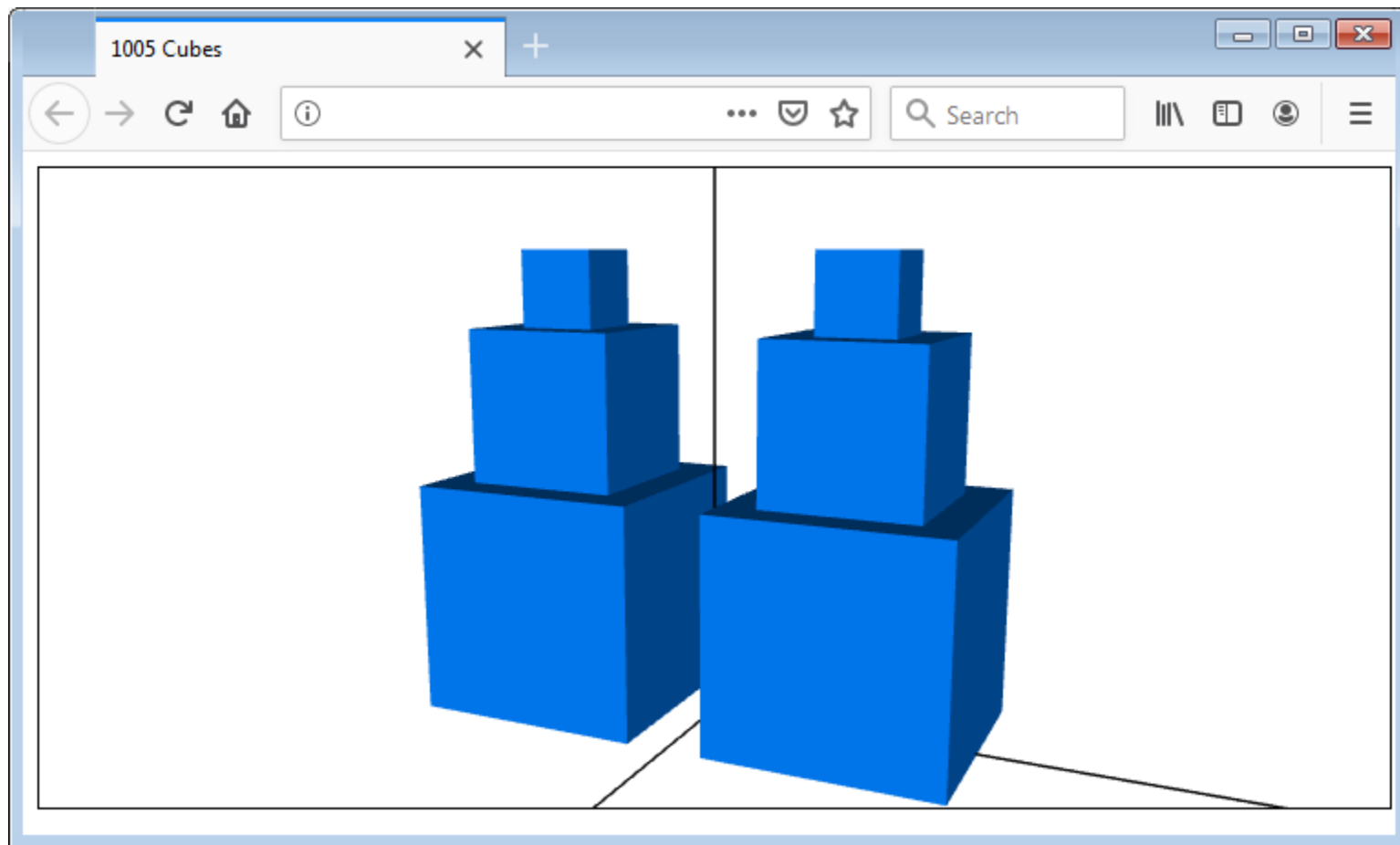
# Example

- Two pyramids of cubes with sizes 3, 2 and 1
- One of the pyramids is with cubes with original origins
- The other pyramid is with cubes with modified origins

```
cube([0, -2, 1.5], 3);  
cube([0, -2, 4.0], 2);  
cube([0, -2, 5.5], 1);
```

```
a = cube([0, 2, 0], 3); a.origin=[0, 0, -1/2];  
a = cube([0, 2, 3], 2); a.origin=[0, 0, -1/2];  
a = cube([0, 2, 5], 1); a.origin=[0, 0, -1/2];
```





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# Cuboid in Suica

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## Cuboid

- Graphical object with properties
- Used to draw cubes and cuboids

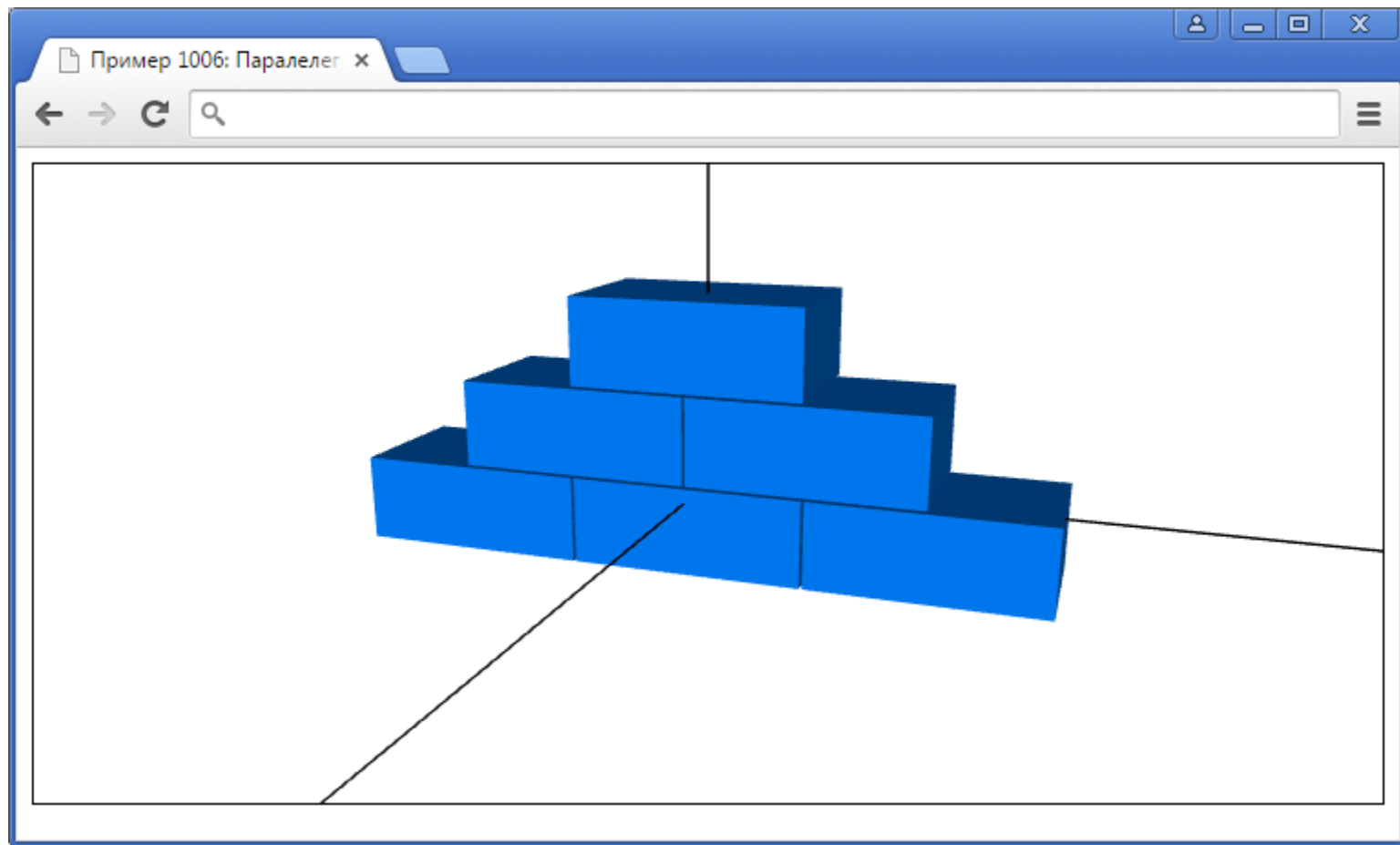
## Creating cuboid

- With class `new Suica.Cuboid ( center, sizes )`
- With function `cuboid ( center, sizes )`
- Center is coordinates of a point, an array of three numbers
- Sizes is an array of three numbers – the lengths of the sides

# Example

- Small wall with 6 bricks of size 8x5x3

```
cuboid([0,0,-1],[5,8,3]);  
cuboid([0,-8.1,-1],[5,8,3]);  
cuboid([0,+8.1,-1],[5,8,3]);  
  
cuboid([0,-4.05,2.1],[5,8,3]);  
cuboid([0,4.05,2.1],[5,8,3]);  
  
cuboid([0,0,5.2],[5,8,3]);
```



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# Orientation

# Object orientation

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## Position

- Visual location of 2D/3D object is determined by properties center and size/sizes

## A problem

- They are not enough
- There is no way to rotate the object

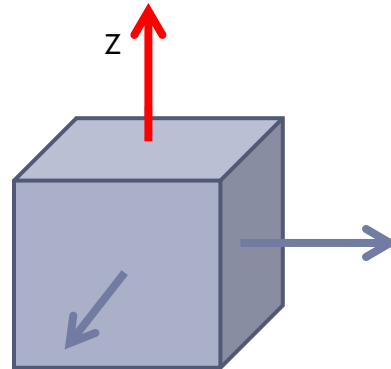
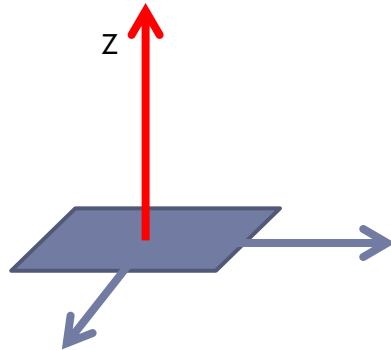


# Implementation of orientation



## Invisible elements

- Every object has a local coordinate system (it is used for the property origin)
- The local Z-axis is used to orient the object

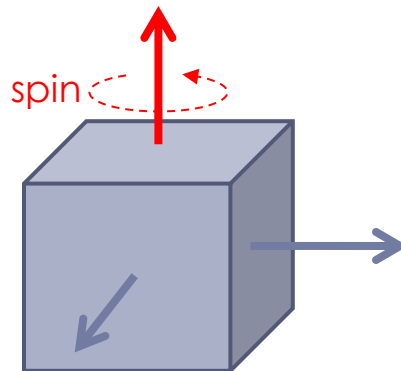
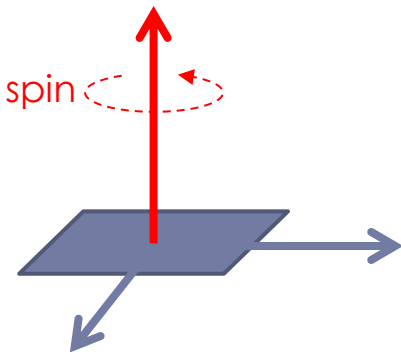


# Properties



## Property spin

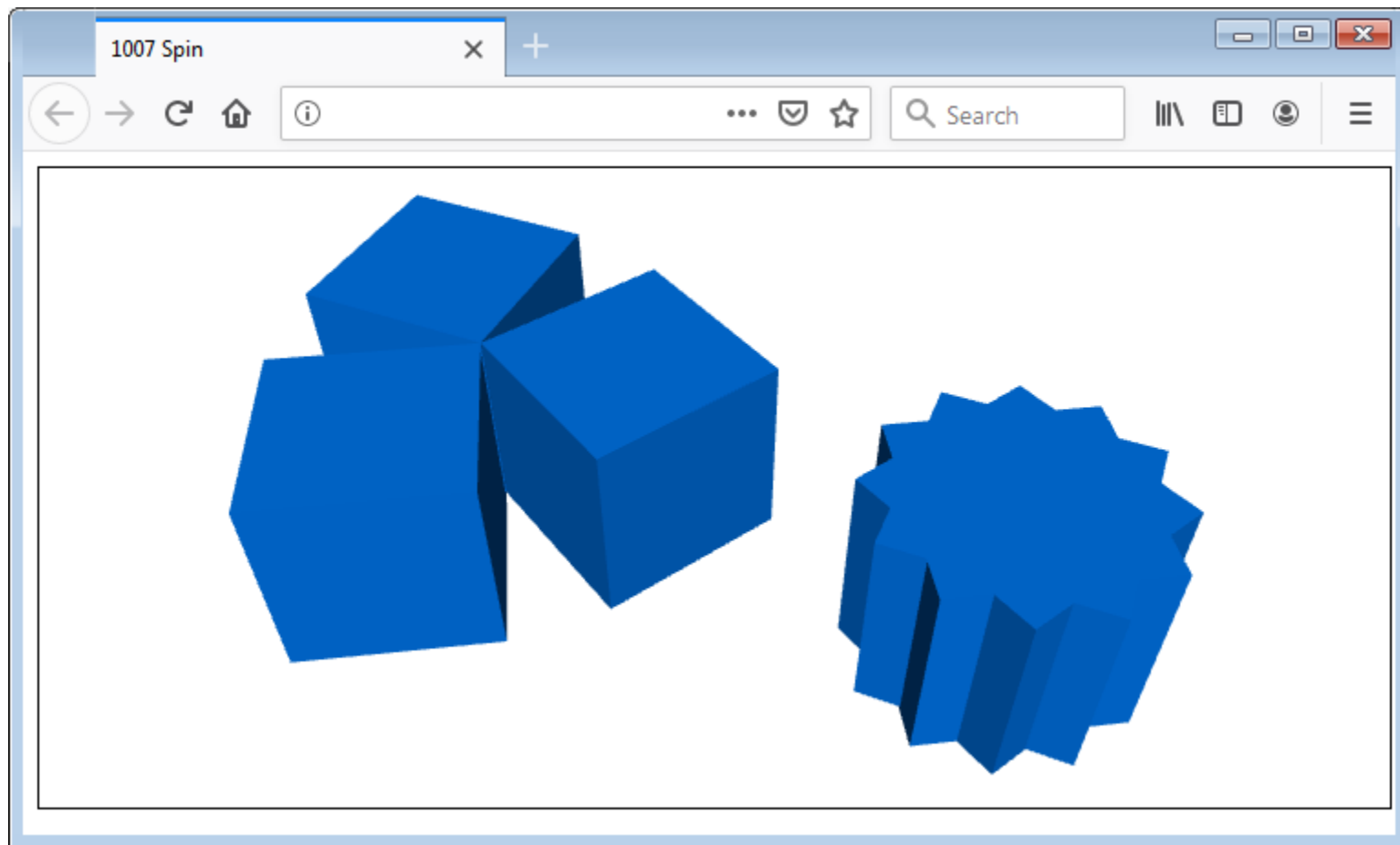
- Rotates the object around the local Z-axis
- The value of **spin** is in radians
- By default it is 0



# Example

- Cubes, rotated around their central axis
- Cubes, rotated around their side edges (done by moving the center to the edge)

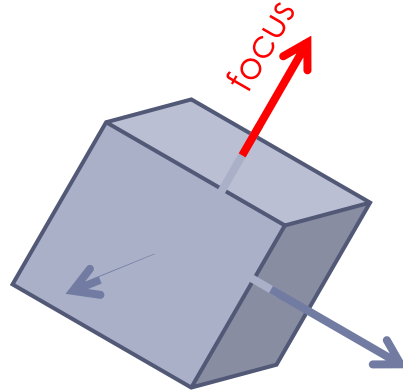
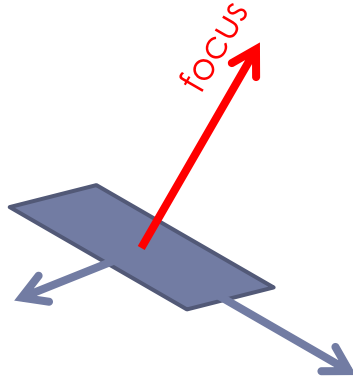
```
a = cube([0,7,0],5);  
a.spin = Math.PI/6;  
:  
a = cube([0,-6,0],5);  
a.origin = [0.5,0.5,0];  
a.spin = 2*Math.PI/3;
```



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# Property focus

- Changes the direction of the local Z-axis
- Also changes the other local axes to maintain orthogonality
- The value of **focus** a vector
- By default it is  $(0,0,1)$  and coincides with the global Z-axis



# Example

- Cube wit multicolour sides – constructed from squares

```
a = square([-3,0,0],6); a.color = [0,0,0];
```

```
a.focus = [-1,0,0];
```

```
a = square([3,0,0],6); a.color = [0,0,1];
```

```
a.focus = [1,0,0];
```

```
a = square([0,-3,0],6); a.color = [0,1,0];
```

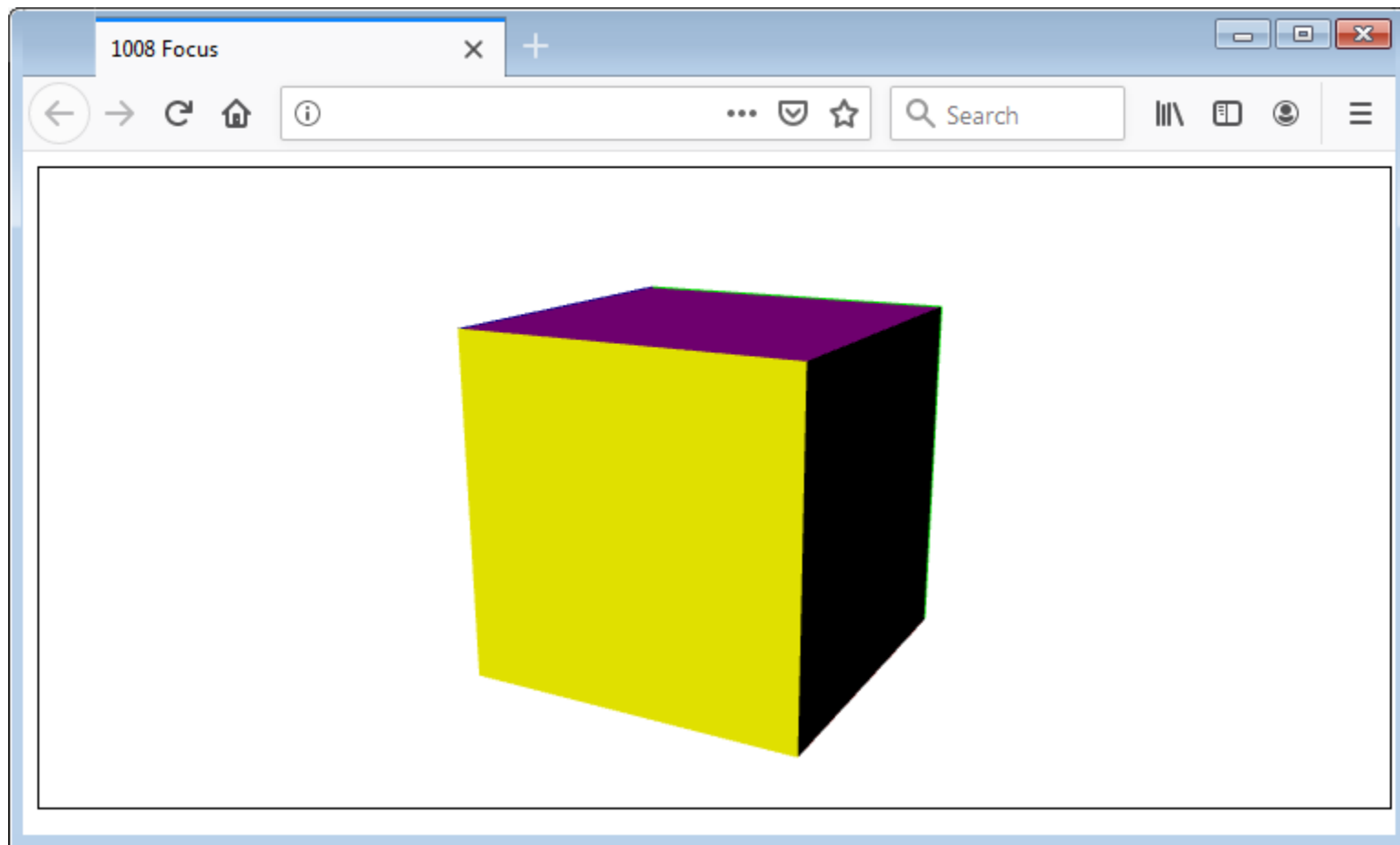
```
a.focus = [0,-1,0];
```

```
a = square([0,3,0],6); a.color = [1,1,0];
```

```
a.focus = [0,1,0];
```

```
a = square([0,0,-3],6); a.color = [1,0,0];
```

```
a = square([0,0,3],6); a.color = [1,0,1];
```



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# Interaction of properties

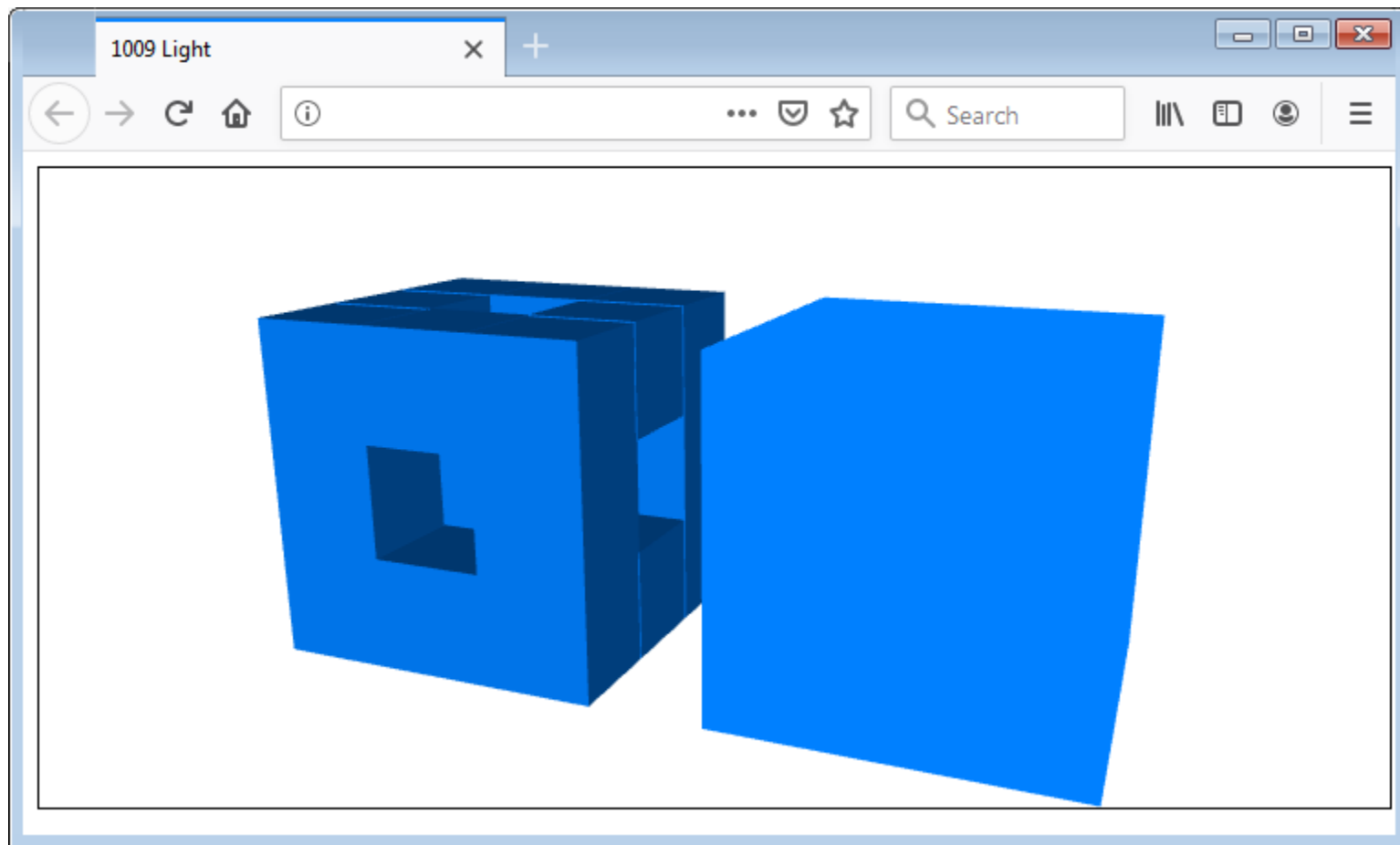
- When orientation is changed by focus, then spin rotates around the new axis
- The vector focus starts from the center of the object, which can be offset by origin
- Not every orientation can be achieved by using only focus, sometimes spin is also needed



# Property light

- Determines whether light shading is used or not used
- When light shading is on, the side surfaces become darker
- When light shading is off, all surfaces use their original colours

```
for (var x=-1; x<=1; x++)  
  for (var y=-1; y<=1; y++)  
    for (var z=-1; z<=1; z++)  
      if (Math.abs(x)+Math.abs(y)+Math.abs(z)!=1)  
      {  
        a = cube([x-2,y,z],1);  
        a = cube([x+2,y,z],1);  
        a.light = false;  
      }
```



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# Examples

# Example №1

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## A pyramid of squares

- Concentric squares one over another
- Their sizes get smaller until they reach 1x1

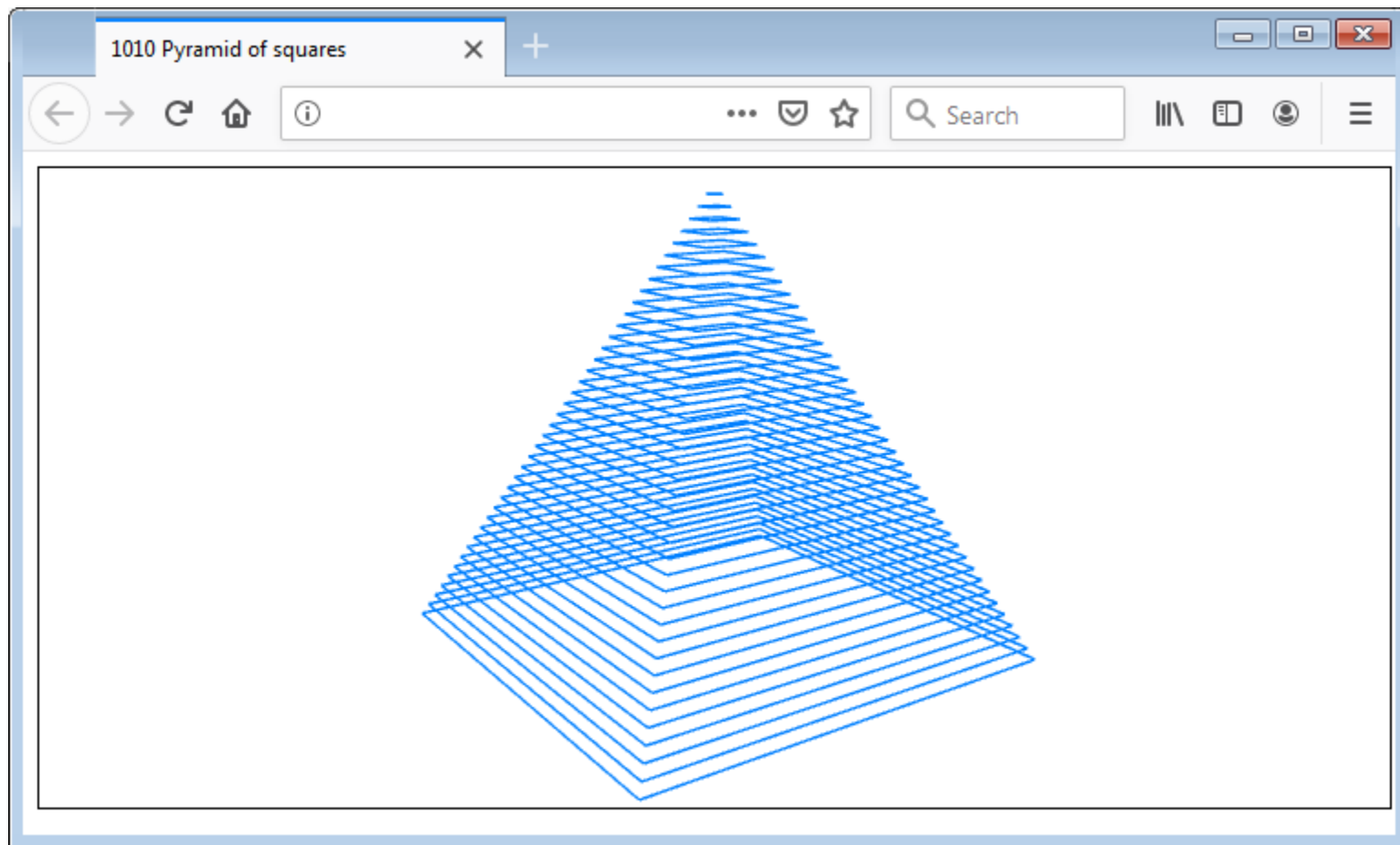
## Idea

- Initial square – the one at the top of the pyramid
- Every next square is increased by 1
- The X and Y coordinates of the center is the same, only Z is decreased by 1

# Solution

- Generating squares top to bottom
- The vertical position of a square is decreasing in **z**
- The size is increasing in **i**

```
n = 40;  
z = 25;  
  
for (var i=1; i<=n; i++)  
{  
    a = square([0,0,z],i);  
    a.mode = Suica.LINE;  
    z--;  
}
```



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# Example №2

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## Glued rectangles

- Two perpendicular lines
- Random rectangles glued to them

## Idea

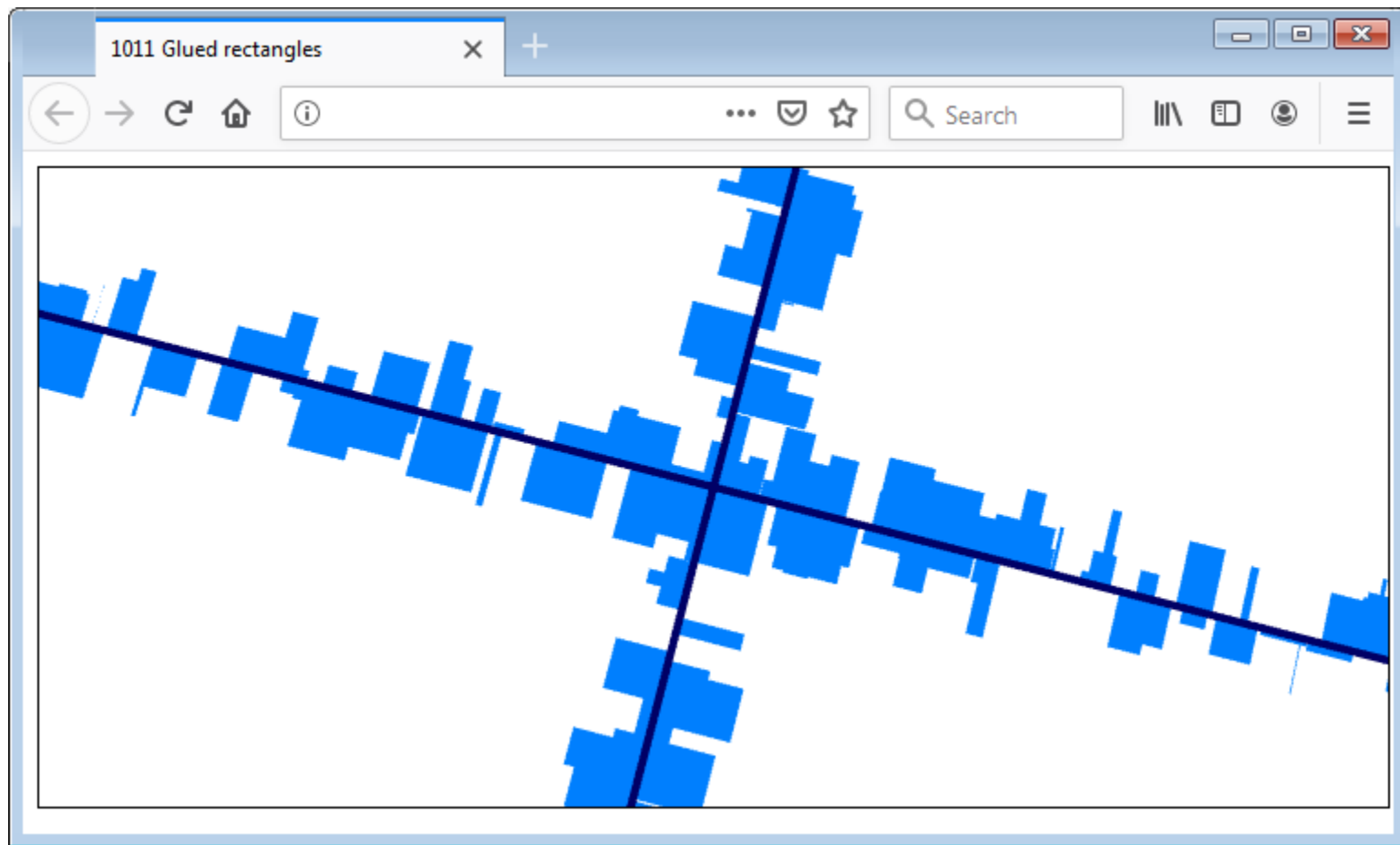
- For convenience the lines are along X and Y axes
- The centers of rectangles are on the lines if origin is properly set

# Solution

- Rectangles have centers  $(x,0,0)$  and  $(0,y,0)$
- For offset use the sign of a random number from -1 to +1
- Rectangles with centers  $(x,0,0)$  have origins  $(0,\pm 1/2,0)$
- Rectangles with centers  $(0,y,0)$  have origins  $(\pm 1/2,0,0)$

```
for (var i=0; i<n; i++)  
{  
  a = rectangle([random(-10,10),0,0],[...]);  
  a.origin = [0,Math.sign(random(-1,1))/2,0];  
  
  a = rectangle([0,random(-10,10),0],[...]);  
  a.origin = [Math.sign(random(-1,1))/2,0,0];  
}
```





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# Example №3

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## Spiral staircase

- Steps are positioned in a spiral

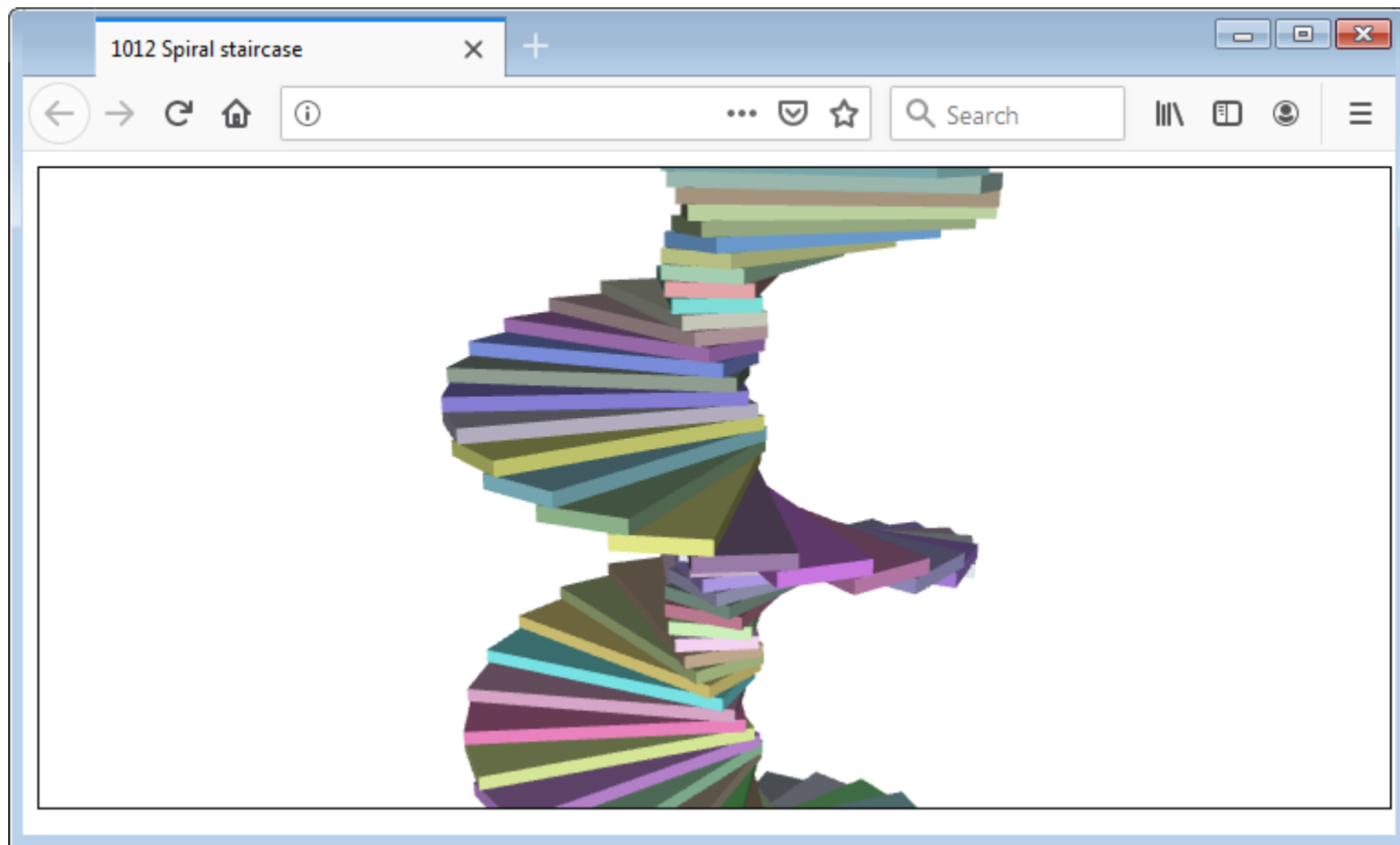
## Idea

- Each step is a flat cuboid
- Their centers are on a vertical line
- Their centers are shifted to make this possible
- Each step is rotated depending on its number

## Solution

- Steps are positioned vertically from -40 to 24
- Their centers are shifted almost to the end of the steps (to 0.4 instead of 0.5)
- Each step is rotated 15 degrees relative to the next step

```
for (var z=-40; z<25; z++)  
{  
  a = cuboid([0,0,z],[20,6,1]);  
  a.origin = [-0.4,0,0];  
  a.color = [random(0.5,1),random(0.5,1),  
             random(0.5,1)];  
  a.spin = z*radians(15);  
}
```



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# Example N°4

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## Sphere of cubes

- Randomly oriented cubes on the surface of a sphere

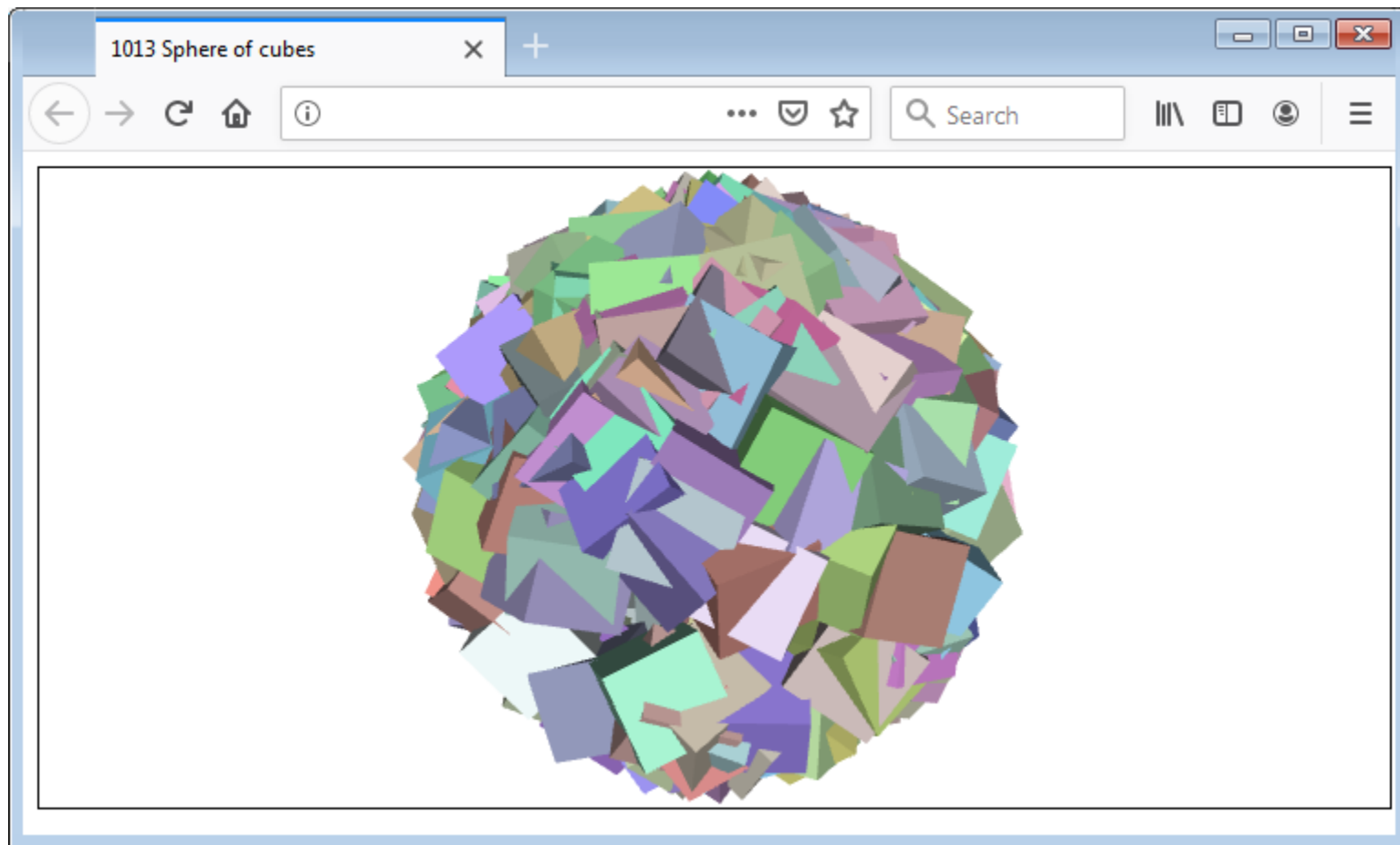
## Idea

- Get two random angles and a fixed radius
- They define a point on the sphere – the position of a cube
- Cube's orientation is random

# Solution

- Transforming spherical coordinates to Cartesian
- Random vector for focus, random angle for spin

```
for (var i=0; i<300; i++)  
{  
    a = random(0,2*Math.PI);  
    b = random(0,2*Math.PI);  
    c = cube([10*Math.cos(a)*Math.cos(b),  
              10*Math.sin(a)*Math.cos(b),  
              10*Math.sin(b)],4);  
    c.color = [random(0.5,1),random(0.5,1),random(0.5,1)];  
    c.spin = random(0,2*Math.PI);  
    c.focus = [random(-1,1),random(-1,1),random(-1,1)];  
}
```



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# Summary



# Graphical objects

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## Square

- Created with `new Suica.Square` or `square`
- Has `center` and `size`
- Supports `mode`, `origin`, `spin`, `focus` and `light`

## Rectangle

- Created with `new Suica.Rectangle` or `rectangle`
- Same properties as the square, except for `sizes` instead of `size`

## Cube

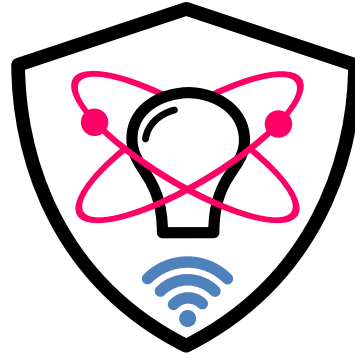
- Created with `new Suica.Cube` or `cube`
- Has `center` and `size`
- Same properties as the square

## Cuboid

- Created with `new Suica.Cuboid` or `cuboid`
- Same properties as the cube, except for `sizes` instead of `size`

# Common properties

- **mode** – drawing mode (**POINT**, **LINE**, **SOLID**)
- **size** – length of the edge of a square or a cube
- **sizes** – lengths of the edges of a rectangle or a cuboid
- **origin** – offset of the object's center
- **spin** – rotation around the local Z-axis
- **focus** – direction of the local Z-axis
- **light** – using or ignoring light shading



**ICT in SES**

**End**

Comments, questions